

$$(1.24 \times 10^3 \text{ J/}^\circ\text{C})t_f = 3.39 \times 10^4 \text{ J}$$

$$t_f = \frac{3.39 \times 10^4 \text{ J}}{1.24 \times 10^3 \text{ J/}^\circ\text{C}}$$

$$= 27.3^\circ\text{C}$$

7. heat gained by water + heat lost by metal = 0

$$\Delta Q_W + \Delta Q_M = 0$$

$$m_W \Delta t_W c_W + m_M \Delta t_M c_M = 0$$

$$(0.265 \text{ kg})(33.0^\circ\text{C} - 26.0^\circ\text{C})(4.18 \times 10^3 \text{ J/kg}\cdot^\circ\text{C}) +$$

$$(0.352 \text{ kg})(33.0^\circ\text{C} - 215^\circ\text{C})c = 0$$

$$7.75 \times 10^3 \text{ J} = (64.1 \text{ kg}\cdot^\circ\text{C})c$$

$$c = \frac{7.75 \times 10^3 \text{ J}}{64.1 \text{ kg}\cdot^\circ\text{C}}$$

$$= 1.21 \times 10^2 \text{ J/kg}\cdot^\circ\text{C}$$

8.  $E_k = \frac{1}{2}mv^2$

$$= \frac{1}{2}(0.101 \text{ kg})(40.0 \text{ m/s})^2$$

$$= 80.8 \text{ J}$$

$$\Delta E_h = m\Delta t c$$

$$\Delta t = \frac{\Delta E_h}{mc}$$

$$= \frac{80.8 \text{ J}}{(0.101 \text{ kg})(4.18 \times 10^3 \text{ J/kg}\cdot^\circ\text{C})}$$

$$= 0.191^\circ\text{C}$$

9. heat gained by cold liquid + heat lost by warm liquid = 0

$$\Delta E_{hc} + \Delta E_{hw} = 0$$

$$m_c \Delta t_c c_c + m_w \Delta t_w c_w = 0$$

$$(20.0 \text{ g})(t_f - 10.0^\circ\text{C})c_c + (29.0 \text{ g})(t_f - 52.0^\circ\text{C})c_w = 0$$

Can divide both sides by  $c$ .

$$\therefore (20.0 \text{ g})(t_f - 10.0^\circ\text{C}) + (29.0 \text{ g})(t_f - 52.0^\circ\text{C}) = 0$$

$$(20.0 \text{ g})t_f - 200.0 \text{ g}\cdot^\circ\text{C} + (29.0 \text{ g})t_f - 1.51 \times 10^3 \text{ g}\cdot^\circ\text{C} = 0$$

$$(49.0 \text{ g})t_f = 1.71 \times 10^3 \text{ g}\cdot^\circ\text{C}$$

$$t_f = \frac{1.71 \times 10^3 \text{ g}\cdot^\circ\text{C}}{49.0 \text{ g}}$$

$$= 34.9^\circ\text{C}$$

Note: We did not need to change the mass to kilograms.

### Lesson 5—Law of Conservation of Mechanical Energy

1.  $\Delta E_k + \Delta E_p = 0$

$$\Delta E_k = -\Delta E_p$$

$$\frac{1}{2}m(v_f^2 - v_0^2) = -mg\Delta h$$

$$\frac{1}{2}(v_f^2 - v_0^2) = -g\Delta h$$

$$\frac{1}{2}((3.2 \text{ m/s})^2 - 0) = -(9.80 \text{ m/s}^2)(\Delta h)$$

$$\Delta h = \frac{\frac{1}{2}(3.2 \text{ m/s})^2}{-9.80 \text{ m/s}^2}$$

$$= -0.52 \text{ m}$$

$\therefore$  object is dropped from a height of 0.52 m

2.  $\Delta E_k + \Delta E_p = 0$

$$\Delta E_k = -\Delta E_p$$

$$\frac{1}{2}m(v_f^2 - v_0^2) = -mg\Delta h$$

$$\frac{1}{2}(v_f^2 - v_0^2) = -g\Delta h$$

$$\frac{1}{2}(v_f^2 - 0) = -(9.80 \text{ m/s}^2)(-8.0 \text{ m})$$

$$v_f = \sqrt{2(-9.80 \text{ m/s}^2)(-8.0 \text{ m})}$$

$$= 13 \text{ m/s}$$

3.  $\Delta E_k + \Delta E_p = 0$

$$\Delta E_k = -\Delta E_p$$

$$\frac{1}{2}m(v_f^2 - v_0^2) = -mg\Delta h$$

$$\frac{1}{2}(v_f^2 - v_0^2) = -g\Delta h$$

$$\frac{1}{2}((37.0 \text{ m/s})^2 - 0) = -(9.80 \text{ m/s}^2)(\Delta h)$$

$$\Delta h = \frac{\frac{1}{2}(37.0 \text{ m/s})^2}{-9.80 \text{ m/s}^2}$$

$$= -69.8 \text{ m}$$

$\therefore$  building was 69.8 m tall

4.  $\Delta E_k + \Delta E_p = 0$

$$\Delta E_k = -\Delta E_p$$

$$\frac{1}{2}m(v_f^2 - v_0^2) = -mg\Delta h$$

$$\frac{1}{2}(v_f^2 - v_0^2) = -g\Delta h$$